



# SPEAKER AUTHENTICATION

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## Introduction:

- To ensure the security of a proper access to private information, passwords or personal identification numbers (PIN) have been used. To further enhance the level of security, biometric features such as signature, fingerprint, hand shape, eye iris, and voice have been considered.
- Speaker Authenticating
  1. Speaker Recognition (by characteristics)
    - speaker verification (SV)
    - speaker identification (SID)
  2. verbal information verification (VIV) (by verbal content)

# Speaker Authentication

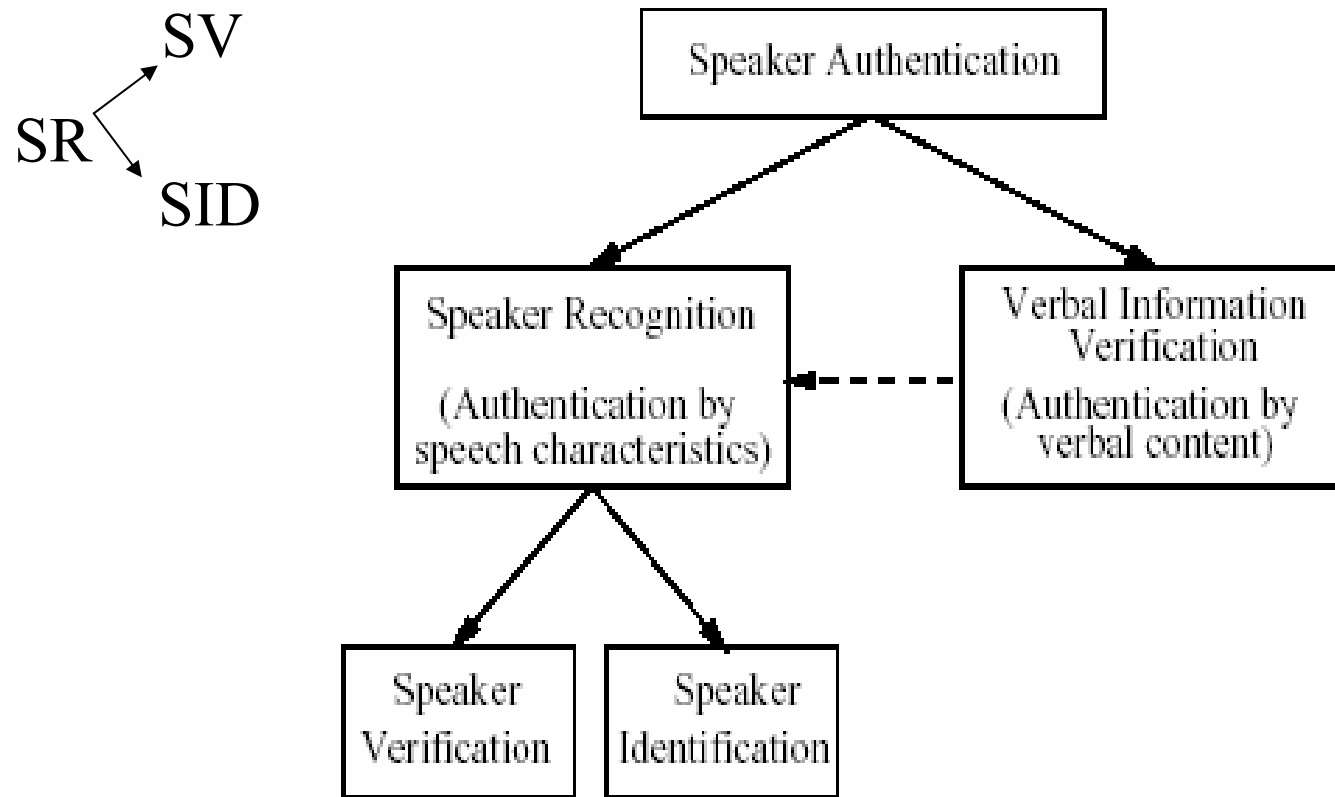


Figure 1.1 Speaker authentication approaches

Multiple-choice classification problem

## Speaker Recognition and Verification

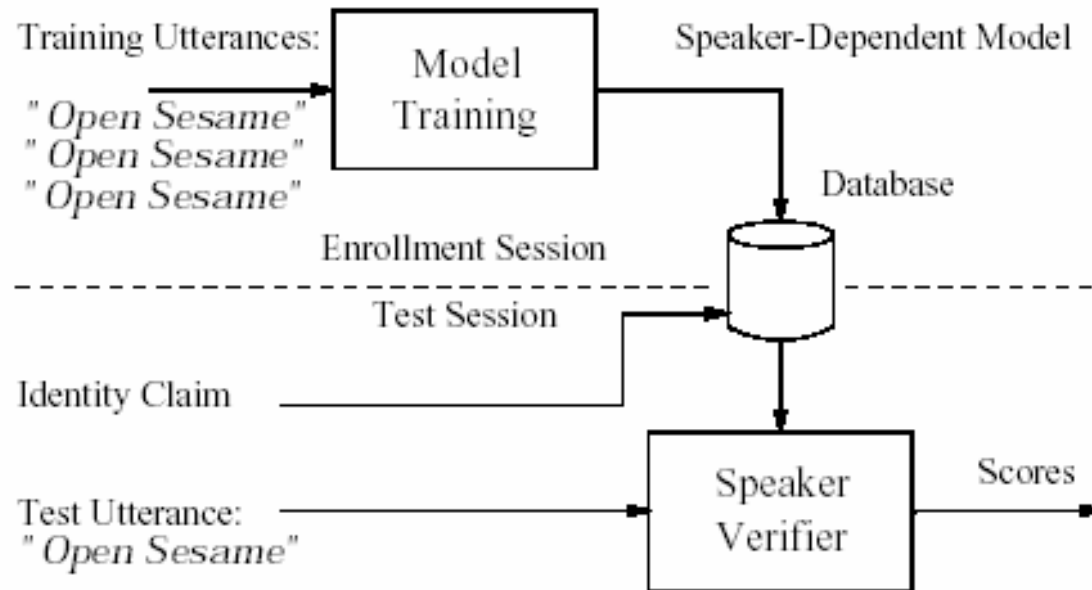


Figure 1.2 A speaker verification system

A typical SV system: enrollment and test sessions.



## Speaker Recognition and Verification (cont.)

### Text-dependent or text-constrained SV systems

#### Fixed pass-phrase system

the spoken digit string is first recognized by an ASR and the standard verification procedure then follows.

#### Text-prompted system (A safety concern)

the system prompts the user to utter a randomized sequence of words in the vocabulary.

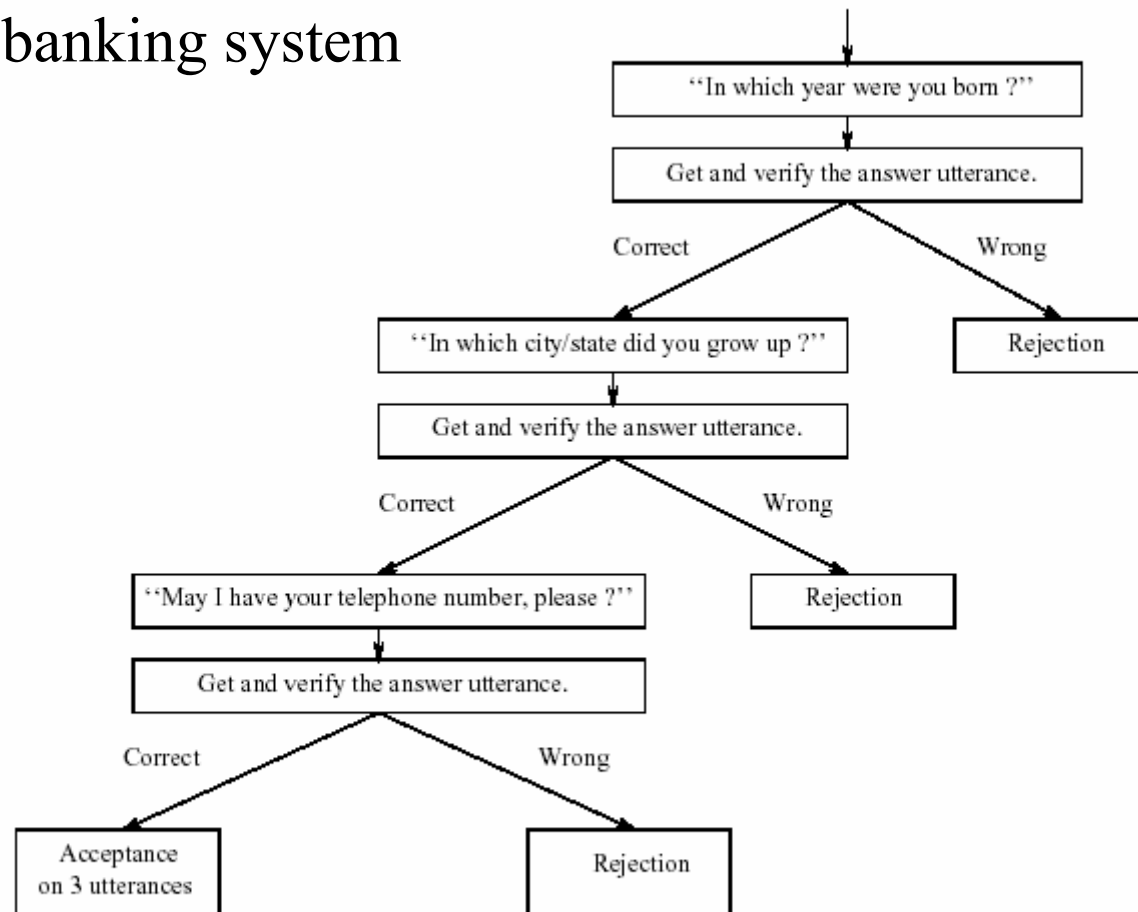


## Verbal Information Verification

- mismatch significantly affects the SV performance
- Enrollment is an inconvenience to the user
- A safety concern

## Verbal Information Verification (cont.)

Tele banking system



**Figure 1.3** An example of verbal information verification by asking sequential questions. (Similar sequential tests can also be applied in speaker verification and other biometric or multi-modality verification.)





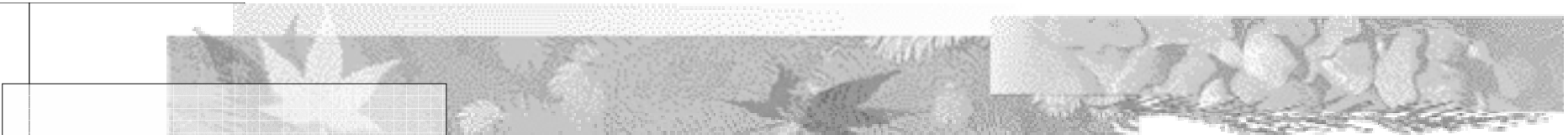
# Pattern Recognition in Speaker Authentication

## Bayesian Decision Theory

the probability of being class  $C_i$  given  $\mathbf{o}$   $P(C_i|\mathbf{o})$  is the posterior probability,  $P(\mathbf{o}|C_i)$  is the conditional probability,  $P(C_i)$  is prior probability:

$$P(C_i|\mathbf{o}) = \frac{P(\mathbf{o}|C_i)P(C_i)}{p(\mathbf{o})}$$

$$p(\mathbf{o}) = \sum_{j=1}^M P(\mathbf{o}|C_j)P(C_j)$$



Let  $L(\alpha_i|C_j)$  be the loss function describing the loss incurred for taking action when the true class is  $C_j$ . The expected risk associated with taking action  $\alpha_i$  is

$$R(\alpha_i|\mathbf{o}) = \sum_{j=1}^M \mathcal{L}(\alpha_i|C_j)P(C_j|\mathbf{o}).$$

$$\mathcal{L}(\alpha_i|C_j) = \begin{cases} 0 & i = j \\ 1 & i \neq j. \end{cases} \quad i, j = 1, \dots, M$$

$$\begin{aligned} R(\alpha_i|\mathbf{o}) &= \sum_{j=1}^M \mathcal{L}(\alpha_i|C_j)P(C_j|\mathbf{o}) \\ &= \sum_{j \neq i} P(C_j|\mathbf{o}) = 1 - P(C_i|\mathbf{o}). \end{aligned}$$


$$\alpha_k = \arg \max_{1 \leq i \leq M} P(C_i | \mathbf{o}).$$

$$\alpha_k = \arg \max_{1 \leq i \leq M} p(\mathbf{o} | C_i) P(C_i).$$

$$P(C_i | \mathbf{O}) = \prod_{t=1}^T P(C_i | \mathbf{o}_t).$$

$$\alpha_k = \arg \max_{1 \leq i \leq M} \prod_{t=1}^T p(\mathbf{o}_t | C_i) P(C_i).$$

$$\alpha_k = \arg \max_{1 \leq i \leq M} \sum_{t=1}^T \log p(\mathbf{o}_t | C_i) P(C_i).$$

## Stochastic Models for Stationary Process

Gaussian mixture model (GMM):

$$p(\mathbf{o}_t | C_j) = p(\mathbf{o}_t | \lambda_j) = \sum_{i=1}^J c_i \mathcal{N}(\mathbf{o}_t; \mu_i, \Sigma_i),$$

$$\mathcal{N}(\mathbf{o}_t; \mu_i, R_i) = \frac{1}{(2\pi)^{d/2} |\Sigma_i|^{1/2}} \exp \left\{ -\frac{1}{2} (\mathbf{o}_t - \mu_i)^T \Sigma_i^{-1} (\mathbf{o}_t - \mu_i) \right\},$$

## Stochastic Models for Stationary Process (cont.)

### EM Algorithm

Given a sequence of feature vectors, the GMM parameters can be estimated iteratively by an expectation-maximization (EM) algorithm [7]. The EM algorithm is based on an auxiliary function  $Q(\cdot)$ . When  $Q(\cdot)$  increases, it guarantees that  $p(\mathbf{O}|\lambda)$  will increase. The EM procedure is as follows:

1. initialize a model  $\lambda^k$ ;
2. in an E-step, evaluate the auxiliary function  $Q(\lambda^k, \lambda^{k-1})$ ;
3. in an M-step, optimize a new model  $\lambda^{k+1}$ , such that  $Q(\lambda^{k+1}, \lambda^k) > Q(\lambda^k, \lambda^{k-1})$ . This implies that  $p(\mathbf{O}|\lambda^{k+1}) \geq p(\mathbf{O}|\lambda^k)$ ; and
4. repeat the above E and M steps until  $Q(\lambda^{k+1}, \lambda^k) - Q(\lambda^k, \lambda^{k-1}) \leq \epsilon$ , where  $\epsilon > 0$  is a pre-selected small number.

## Stochastic Models for Stationary Process (cont.)

### EM Algorithm

$$\hat{c}_i = \frac{1}{T} \sum_{t=1}^T P(z_i | \mathbf{o}_t, \lambda) \quad (1.14)$$

$$\hat{\mu}_i = \frac{\sum_{t=1}^T P(z_i | \mathbf{o}_t, \lambda) \mathbf{o}_t}{\sum_{t=1}^T P(z_i | \mathbf{o}_t, \lambda)} \quad (1.15)$$

$$\hat{\Sigma}_i = \frac{\sum_{t=1}^T P(z_i | \mathbf{o}_t, \lambda) (\mathbf{o}_t - \hat{\mu}_i)(\mathbf{o}_t - \hat{\mu}_i)^T}{\sum_{t=1}^T P(z_i | \mathbf{o}_t, \lambda)} \quad (1.16)$$

where

$$P(z_i | \mathbf{o}_t, \lambda) = \frac{p(\mathbf{o}_t | \lambda) c_i}{\sum_{j=1}^J P(\mathbf{o}_t | \lambda) c_j}. \quad (1.17)$$



## Stochastic Models for Stationary Process (cont.)

When Testing: assume **the prior is the same** for all speakers  
Take action

$$\alpha_k = \arg \max_{1 \leq i \leq M} \sum_{t=1}^T \log p(\mathbf{o}_t | \lambda_i).$$

## Stochastic Models for Non-Stationary Process

The stationary process ignored the temporal information. In other applications, such as speaker verification, the temporal information is necessary in making decisions.

A more powerful model, Hidden Markov Model (HMM) is then applied to characterize both the temporal structure and the corresponding statistical variations along the trajectory of an utterance.

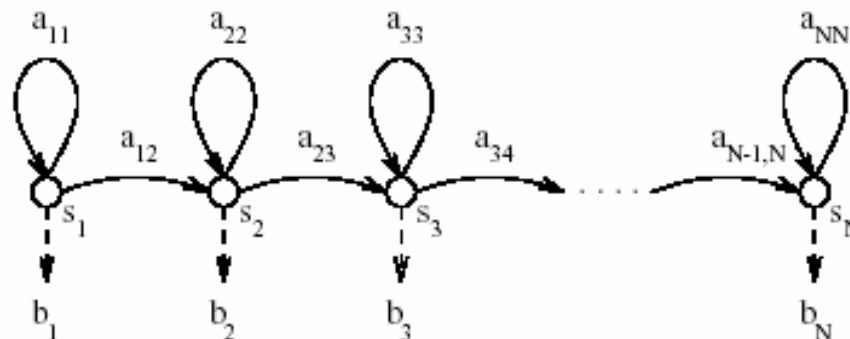



Figure 1.4 Left-to-right hidden Markov model.





## Stochastic Models for Non-Stationary Process(cont.)

Speech Segmentation

Viterbi Algorithm

$$P(\mathbf{O}, s_{\max} | \lambda) = \max_{\{s_t\}} \left\{ \prod_{t=1}^T a_{s_{t-1}s_t} b_{s_t}(\mathbf{O}_t) \right\}$$

## Statistical Verification

$$R(\alpha_1|\mathbf{o}) = \mathcal{L}(\alpha_1|C_1)P(C_1|\mathbf{o}) + \mathcal{L}(\alpha_1|C_2)P(C_2|\mathbf{o}) \quad (1.21)$$

$$R(\alpha_2|\mathbf{o}) = \mathcal{L}(\alpha_2|C_1)P(C_1|\mathbf{o}) + \mathcal{L}(\alpha_2|C_2)P(C_2|\mathbf{o}) \quad (1.22)$$

The action  $\alpha_1$  corresponds to decide that the true class is class  $C_1$  if

$$R(\alpha_1|\mathbf{o}) < R(\alpha_2|\mathbf{o}). \quad (1.23)$$

Bring (1.21) and (1.22) into(1.23) and rearranging the terms, we take action  $\alpha_1$  if:

$$\frac{P(C_1|\mathbf{o})}{P(C_2|\mathbf{o})} > \frac{\mathcal{L}(\alpha_1|C_2) - \mathcal{L}(\alpha_2|C_2)}{\mathcal{L}(\alpha_2|C_1) - \mathcal{L}(\alpha_1|C_1)} = \mathcal{T}_1 \quad (1.24)$$

where  $\mathcal{T}_1 > 1$  is a threshold. Furthermore, if we apply the Bayes formula to replace the posterior probabilities by prior probabilities, we have

$$\frac{p(\mathbf{o}|C_1)}{p(\mathbf{o}|C_2)} > \mathcal{T}_1 \frac{P(C_2)}{P(C_1)} = \mathcal{T}_2. \quad (1.25)$$

For a sequence of observation  $\mathbf{O} = \{\mathbf{o}_t\}_{t=1}^T$ , if we assume that the distributions of the observations are independent, we have the likelihood-ratio:

$$r(\mathbf{O}) = \frac{\prod_{t=1}^T p(\mathbf{o}_t|C_1)}{\prod_{t=1}^T p(\mathbf{o}_t|C_2)} = \frac{P(\mathbf{O}|C_1)}{P(\mathbf{O}|C_2)} > \mathcal{T}_3. \quad (1.26)$$



## Statistical Verification (cont.)

In practice, we compute log-likelihood ratio for verification:

$$\mathcal{R}(\mathbf{O}) = \log P(\mathbf{O}|C_1) - \log P(\mathbf{O}|C_2), \quad (1.27)$$

A decision is made as:

$$\begin{cases} \text{Acceptance: } \mathcal{R}(\mathbf{O}) \geq \mathcal{T}; \\ \text{Rejection: } \mathcal{R}(\mathbf{O}) < \mathcal{T}; \end{cases} \quad (1.28)$$

where  $\mathcal{T}$  is a threshold value, which can be determined theoretically or experimentally.



## Statistical Verification (cont.)

False rejection : rejecting the hypothesis when it is actually true.

False acceptance: accepting it when it is actually false.

Equal error rate: the error rate when the operating point is so chosen as to achieve equal error probabilities for the two types of error.

# Speaker Authentication System

## Speaker Verification

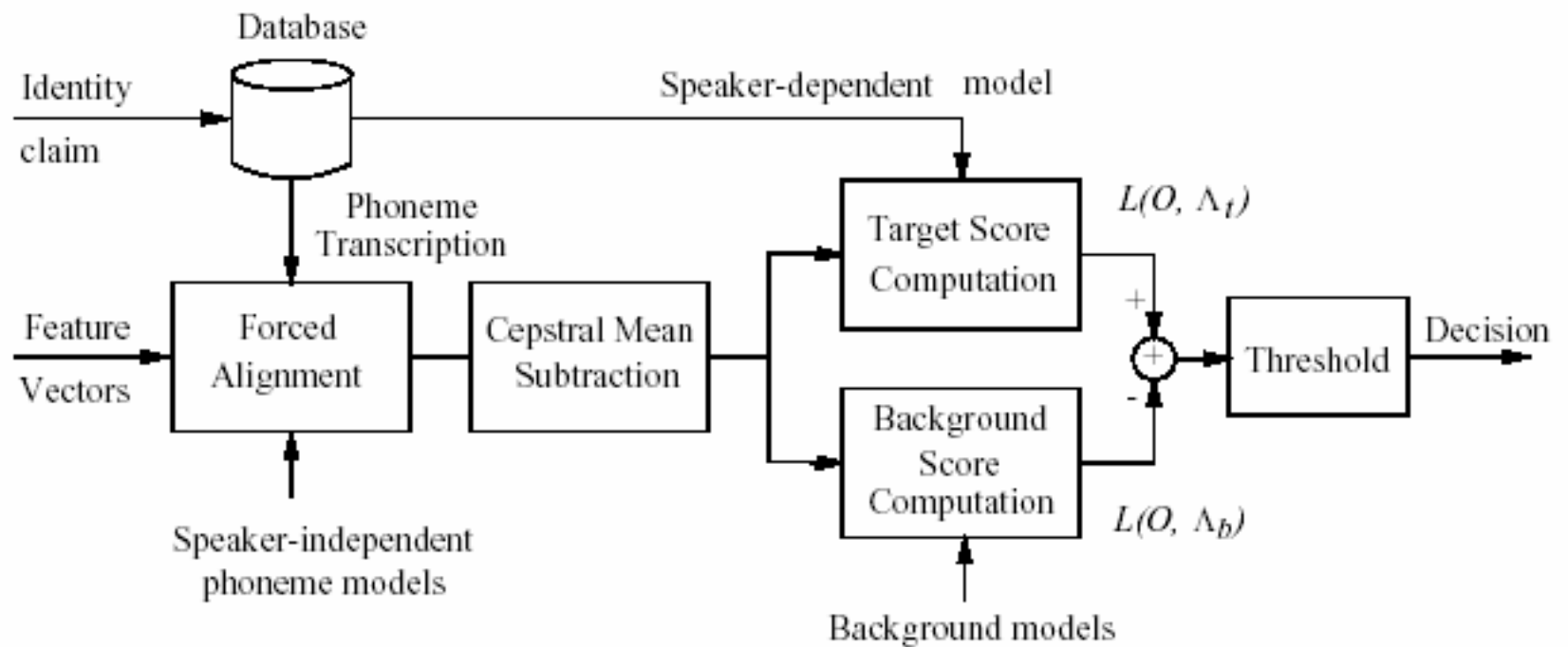


Figure 1.5 A fixed-phrase speaker verification system

## Speaker Authentication System (cont.)

VIV : with UV

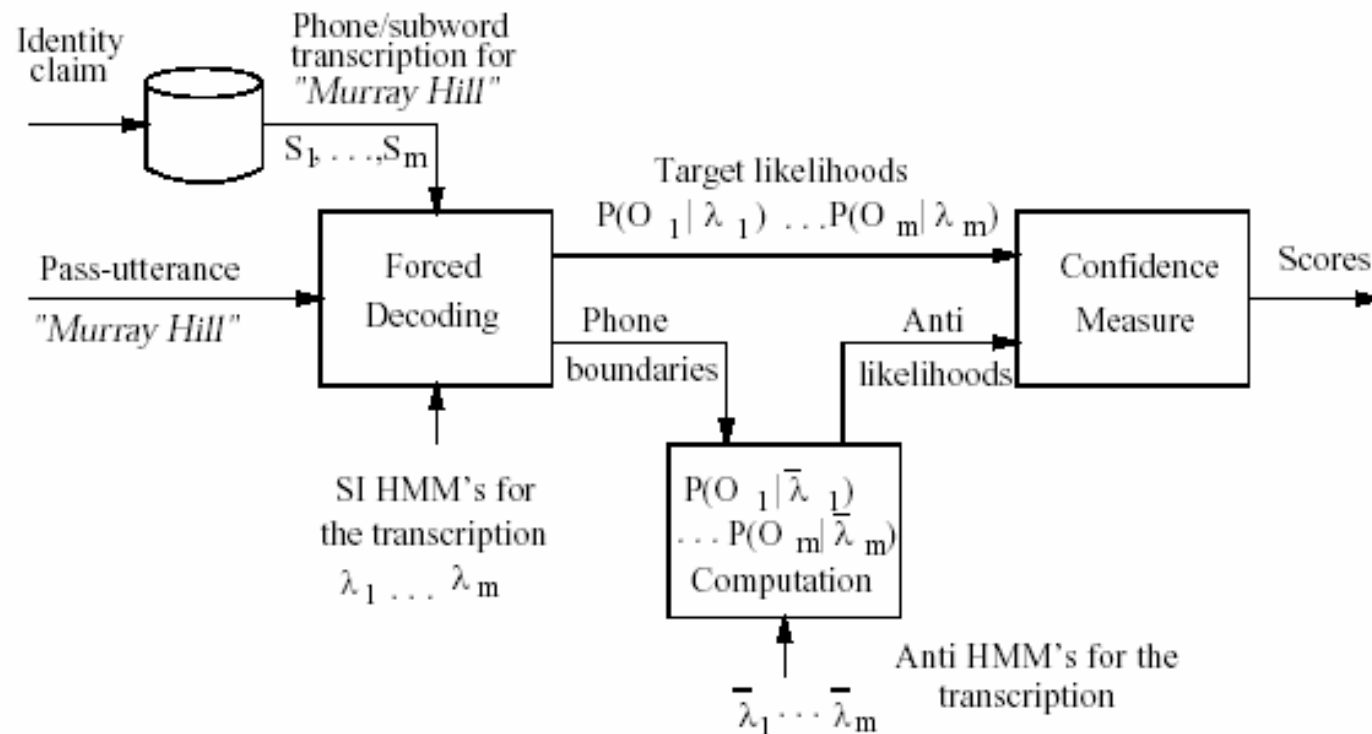


Figure 1.6 Utterance verification in VIV



## Speaker Authentication System (cont.)

Utterance Segmentation

Subword Hypothesis Testing

Confidence Measure Calculation

Sequential Utterance Verification



## Speaker Authentication System (cont.)

### Utterance Segmentation

$$P(\mathbf{O}|\mathbf{S}) = \max_{T_1, T_2, \dots, T_N} P(O_1^{T_1} | S_1) P(O_{T_1+1}^{T_2} | S_2) \dots P(O_{T_{N-1}+1}^{T_N} | S_N), \quad (1.32)$$

where

$$\mathbf{O} = \{\mathbf{O}_1, \mathbf{O}_2, \dots, \mathbf{O}_N\} = \{O_1^{T_1}, O_{T_1+1}^{T_2}, \dots, O_{T_{N-1}+1}^{T_N}\}, \quad (1.33)$$



## Speaker Authentication System (cont.)

### Subword Hypothesis Testing

$$r(\mathbf{O}_n) = \frac{P(\mathbf{O}_n|H_0)}{P(\mathbf{O}_n|H_1)} = \frac{P(\mathbf{O}_n|\lambda_n)}{P(\mathbf{O}_n|\bar{\lambda}_n)}, \quad (1.34)$$

$$R(\mathbf{O}_n) = \log P(\mathbf{O}_n|\lambda_n) - \log P(\mathbf{O}_n|\bar{\lambda}_n). \quad (1.35)$$

$$R_n = \frac{1}{T_n} [\log P(\mathbf{O}_n|\lambda_n) - \log P(\mathbf{O}_n|\bar{\lambda}_n)], \quad (1.36)$$

$$\begin{cases} \text{Acceptance:} & R_n \geq \mathcal{T}_{n\bar{c}} \\ \text{Rejection:} & R_n < \mathcal{T}_{n\bar{c}} \end{cases} \quad (1.37)$$

## Speaker Authentication System (cont.)

### Confidence Measure Calculation

$$M(\mathbf{O}) = F(R_1, R_2, \dots, R_N), \quad (1.38)$$

$$M_1 = \frac{1}{L} \sum_{n=1}^N l_n R_{n1} \quad (1.39)$$

$$M_2 = \frac{1}{N} \sum_{n=1}^N R_{n1} \quad (1.40)$$

$$C_n = \frac{\log P(\mathbf{O}_n | \lambda_n) - \log P(\mathbf{O}_n | \bar{\lambda}_n)}{\log P(\mathbf{O}_n | \lambda_n)} \quad (1.41)$$

$$M = \frac{1}{N} \sum_{n=1}^N f(C_n), \quad (1.42)$$

where

$$f(C_n) = \begin{cases} 1, & \text{if } C_n \geq \theta; \\ 0, & \text{otherwise,} \end{cases} \quad (1.43)$$

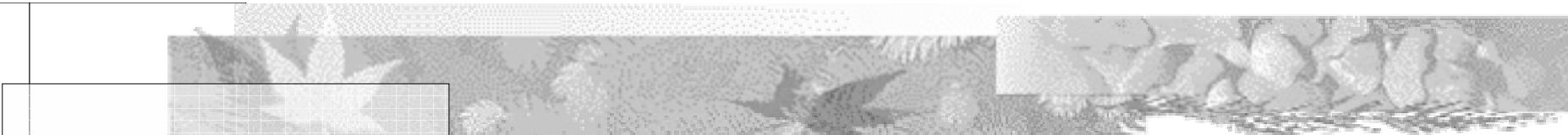
## Speaker Authentication System (cont.)

### Sequential Utterance Verification

$$\mathcal{H}_0 = \bigcap_{i=1}^J H_0(i), \quad (1.44)$$

$$\mathcal{H}_1 = \bigcup_{i=1}^J H_1(i), \quad (1.45)$$

$$\begin{cases} \text{Acceptance:} & M(i) \geq \mathcal{T}(i); \\ \text{Rejection:} & M(i) < \mathcal{T}(i); \end{cases} \quad (1.46)$$


$$\varepsilon_r(\hat{x}) = P( M(\hat{x}) \in \mathcal{R}_1(\hat{x}) \mid H_0(\hat{x}) ), \quad (1.47)$$

and

$$\varepsilon_a(\hat{x}) = P( M(\hat{x}) \in \mathcal{R}_0(\hat{x}) \mid H_1(\hat{x}) ), \quad (1.48)$$

respectively. Furthermore, the FR error on  $J$  utterances can be evaluated as

$$\begin{aligned} E_r(J) &= P\left( \bigcup_{i=1}^J \{M(\hat{x}) \in \mathcal{R}_1(\hat{x})\} \mid \mathcal{H}_0 \right), \\ &= 1 - \prod_{i=1}^J (1 - \varepsilon_r(\hat{x})), \end{aligned} \quad (1.49)$$

and the FA error on  $J$  utterances is

$$\begin{aligned} E_a(J) &= P\left( \bigcap_{i=1}^J \{M(\hat{x}) \in \mathcal{R}_0(\hat{x})\} \mid \mathcal{H}_1 \right), \\ &= \prod_{i=1}^J \varepsilon_a(\hat{x}). \end{aligned} \quad (1.50)$$

## Speaker Authentication System (cont.)

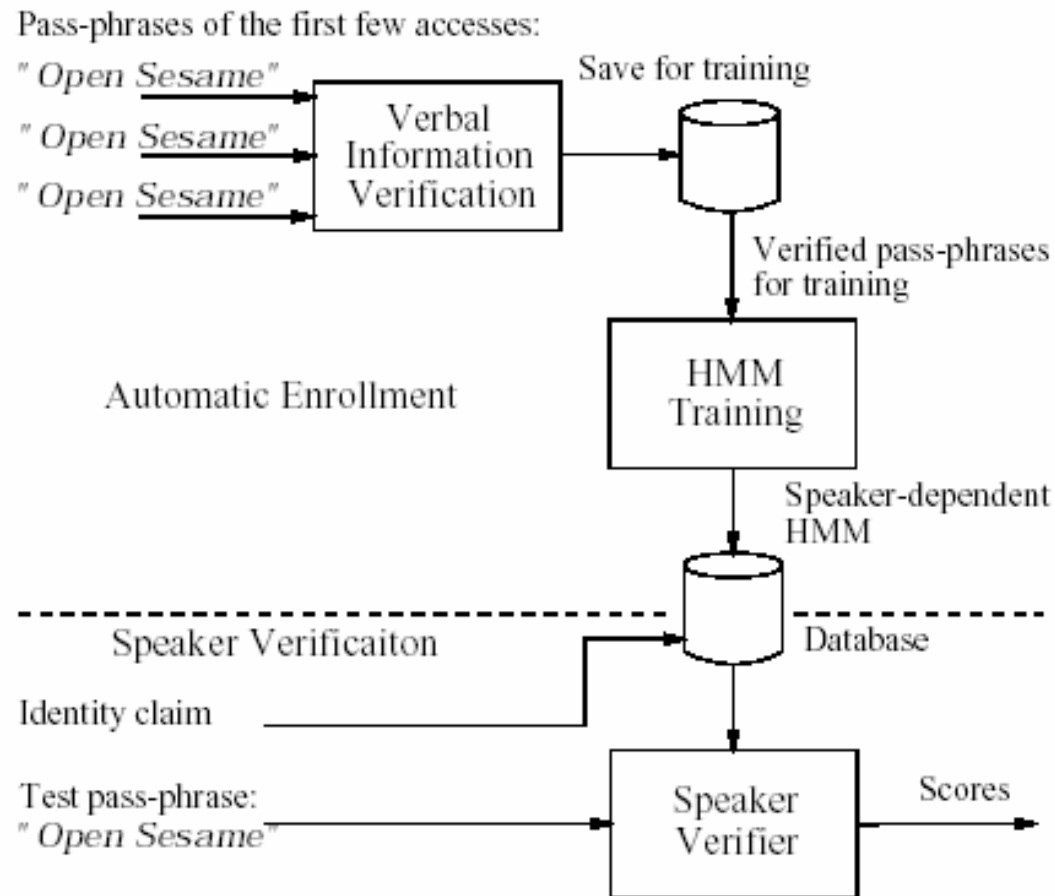


Figure 1.7 The proposed system by combining VIV with speaker verification



## Speaker Authentication System (cont.)

### Experimental Results

**Figure 1.7 Experimental Results without Adaptation in Average Equal-Error Rates**

Algorithms	Individual Thresholds	Pooled Thresholds
SV (Baseline)	3.03 %	4.96 %
VIV+SV(proposed)	1.59 %	2.89 %

**Figure 1.7 Experimental Results with Adaptation in Average Equal-Error Rates**

Algorithms	Individual Thresholds	Pooled Thresholds
SV (Baseline)	2.15 %	3.12 %
VIV+SV(proposed)	1.20 %	1.83 %



## Conclusion

**Depend on Bayesian decision theory and hypothesis testing, the hypothesis testing may be conducted at phrase, word, phoneme, or subword levels.**

**On extension to the Bayesian theory to authentication is the sequential verification procedure, which can also be applied to speaker verification to achieve even lower equal error rates.**

**Currently, the fixed phrase SV system is more attractive to real applications due to its good performances. it is easy to remember and convenient to use.**

**since VIV is to verify the verbal content instead of the voice characteristics, it is users' responsibility to protect their personal information from impostors**



**To improve the user convenience and system performance, the VIV and SV is combined to construct a convenient speaker authentication system.**

**The combined system is convenient to users since they can start to use the system without going through a formal enrollment session and waiting for model training. On the other hand, since the training data could be collected from different channels in different VIV sessions, the acoustic mismatch problem is mitigated, potentially leading to a better system performance in test sessions.**

**The SD HMM's can be updated to cover different acoustic environments while the system is in use to further improve the system performance.**

**VIV can also be used to ensure training data for SV.**